Determination of the upper limit on $m_{\nu_{\tau}}$ from LEP.

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A review of the direct determinations of the upper limit on the tau-neutrino mass from the LEP experiments is given. The experimental methods, the results and the comparison with non LEP measurements are also discussed. The study of the systematic errors shows that the LEP results are statistically limited so that their combination will improve the sensitivity to a massive tau-neutrino. An unofficial combination of the ALEPH and OPAL measurements gives a 95 % confidence level upper limit of 15 MeV/c on m_{ν_τ} .

I. INTRODUCTION: MOTIVATION AND INDIRECT CONSTRAINTS.

The neutrino masses are one of the most puzzling and hot subject of discussion in the high energy physics community. It is believed that the smallness the neutrinos masses can be explained by assuming that they are produced by the mixing between *standard* Dirac mass terms and large Majorana mass terms; the Majorana masses are related to a new energy scale at which the lepton number conservation is violated. This is the so called *see-saw* [1] mechanism which is present in many grand-unified models. If the Standard Model mass hierarchy is preserved in the Dirac sector of the neutrino mass matrix the tau-neutrino is expected to be by far the heaviest neutrino. Under this assumption the neutrino mass hierarchy is expected to be of the order $m_{\nu\tau}: m_{\nu\mu}: m_{\nu e} = m_t^2: m_c^2: m_u^2$.

Cosmology [2] can put strong constraints on the neutrino masses because of their influence on the actual density of the universe. An unstable tau-neutrino with a mass of the order of 10-20 MeV can survive to the cosmological constraints. Measurements of light nucleus abundances which results from Big Bang Nuleo Synthesis [3] can give information on the neutrino masses. The incompatibility between the BBNS prediction and the measured D and H³ abundances can be solved by and unstable tau-neutrino with a mass of the order of 10-25 MeV [4].

The claimed superK [5] discovery of atmospheric neutrinos oscillation would constrain $m_{\nu_{\tau}}$ to be lighter than about 170 KeV (which is the direct limit on the mu-neutrino mass) if what they observe is an oscillation between tau and mu neutrinos.

II. THE FIT TO $m_{\nu_{\tau}}$: 2-DIMENSIONAL METHOD

The $m_{\nu_{\tau}}$ measurements at LEP are based on a fit to the E_h, M_h spectrum in hadronic tau decays. This method has been introduced for the first time by two LEP experiments OPAL [6] and ALEPH [7]. The fact that for each given hadronic mass the hadronic energy is constrained between the two values $E_h^{max,min}(M_h, m_{\nu_{\tau}})$ gives a sizable improvement in the sensitivity to the tau-neutrino mass with respect to the one obtained by a fit to the M_h spectrum alone, as explained in [8,9].

The two decays used at LEP are $\tau \to 5\pi^{\pm}\nu_{\tau}$ and $\tau \to 3\pi^{\pm}\nu_{\tau}$. The first decay mode benefits of a invariant mass spectrum which extends to large values but is limited by the very small branching which is of the order of 0.08%. The second mode benefit of a large statistics (BR($\tau \to 3\pi^{\pm}\nu_{\tau}$)~9%) but the M_h spectrum is suppressed at values close to M_{τ} because of the a_1 dominance in 3π tau decays. The two modes have similar sensitivities even though the regions in the M_h , E_h plane from which this sensitivity comes are slightly different: for the five-prong mode it comes from few events at very high values of M_H and E_h while for the three-prong mode events at very high energy and intermediate mass can contribute too.

The value of $m_{\nu_{\tau}}$ is obtained by a likelihood fit to the observed events where the likelihood has the following form:

$$\mathcal{L}(m_{\nu}) = \prod_{events} \frac{1}{\Gamma} \cdot \frac{d^{2}\Gamma}{dE_{h}dm_{h}} \otimes \mathcal{G}(E_{beam}, E_{\tau}) \otimes \mathcal{R}(m_{h}, E_{h}, \rho, \sigma_{m_{h}}, \sigma_{E_{h}}, ...) \otimes \varepsilon(m_{h}, E_{h})$$
(1)

The $\frac{d^2\Gamma}{dE_hdm_h}$ is the double-differential tau decay width and contains the unknown part related to the hadronic spectral functions. The knowledge of these function is relevant in estimating the sensitivity of an experiment (the so called *luck factor*) but it doesn't affect the limit which comes from a region of the M_h , E_h plane where the phase space is dominant (this is true if no narrow resonance is present with $M_{res} \sim M_{\tau}$ as discussed in the three-prong results section). The effect of initial/final state radiation is described by $\mathcal{G}(E_{beam}, E_{\tau})$; at LEP ISR is expected to be small and it has practically very small effect on the $m_{\nu_{\tau}}$ determination.

The resolution function $\mathcal{R}(m_h, E_h, \rho, \sigma_{m_h}, \sigma_{E_h}, ...)$ is the most delicate part of this measurement; the determination of the M_h, E_h end-point requires the knowledge of the tracking calibration with an accuracy better than the ratio $m_{\nu_{\tau}}/M_{\text{tau}}$. As will be shown in the result section this is the main source of systematics for all the LEP experiments. The detector efficiency is contained in the function $\varepsilon(m_h, E_h)$; since this function is not expected to vary rapidly in the sensitive region its influence on the $m_{\nu_{\tau}}$ determination is expected to be very small.

III. THE RESULTS

In this section the LEP results from five- and three-prong tau decays are reviewed. In the three-prong section the possible problem caused by the presence of a narrow resonance close to the hadronic mass end-point is discussed. Finally the ALEPH and OPAL results are combined with the likelihood product method by using the published five- and three-prong likelihoods. An estimate of the systematic error of the combined result is given too.

A. Results form $\tau \to 5\pi^{\pm}\nu_{\tau}$ tau decays

The decay $\tau \to 5\pi^{\pm}\nu_{\tau}$ decay mode has been used by ALEPH [7] and by OPAL [6] to measure the tau-neutrino mass. Both experiments have analysed the full LEP1 statistics which corresponds to about 200k tau-pairs.

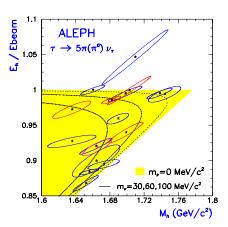


FIG. 1. The five-prong ALEPH events in the M_h, E_h mass planes. The iso-lines corresponding to the kinematic region allowed for a 30, 60 and 100 MeV tau-neutrino are superimposed.

The ALEPH experiment has selected $52 \tau \to 5\pi^{\pm}\nu_{\tau}$ decays (and $3 \tau \to 5\pi^{\pm}\pi^{0}\nu_{\tau}$ decays which due to the worse π^{0} energy resolution have very small impact on the final result) with an efficiency of about 27% and a background from dangerous topologies at the level of 0.6%. In terms of the $m_{\nu_{\tau}}$ upper limit the dangerous backgrounds are the tau decays in which the hadronic mass and/or the hadronic energy are reconstructed at values larger than the true ones. For example a decay $\tau \to 3\pi^{\pm}\pi^{0} \to 3\pi^{\pm}\gamma e^{+}e^{-}$ where the two electrons are reconstructed as pions tends to have a reconstructed hadronic mass which is systematically higher than the true one. If this events are not rejected they could mimic a massless tau-neutrino giving a fake good limit on $m_{\nu_{\tau}}$. The same problem holds for $q\bar{q}$ events

reconstructed as $\tau \to 5\pi^{\pm}\nu_{\tau}$; in fact this kind of events tends to be in the high M_h, E_h region. The typical ALEPH resolutions are of about 15 MeV for M_h and 350 MeV for E_h . The resolution parameters have been determining by using the so called Monte Carlo *cloning* technique [7] which allows the determination of these parameters on an event by event basis.

The fit to the ALEPH events showed in Fig.1 gives a limit of $m_{\nu_{\tau}} < 22.3$ MeV at 95% confidence level. The systematic error is dominated by the knowledge of the parameters of the resolution function. The energy and the mass scales and resolutions have been determined by using the $Z \to \mu^+\mu^-$ events and the charm decays $D^0 \to K^-\pi^+$, $D^0 \to K^-\pi^+\pi^+\pi^-$ and $D^+ \to K^-\pi^+\pi^+$. By adding linearly the 0.8 MeV systematic error the final 95 % C.L. limit is $m_{\nu_{\tau}} < 23.1$ MeV.

The OPAL experiment has performed a similar measurement by selecting $22 \tau \to 5\pi^{\pm}\nu_{\tau}$ decays [6]. The selection efficiency is of 9.3% with a dangerous background of the order of 2.5%. The parameters of the resolution function have been determined, as for ALEPH, with the Monte Carlo cloning technique. In the OPAL paper is proved that this technique is able to spot events with reconstruction problem as shown in Fig. 2.

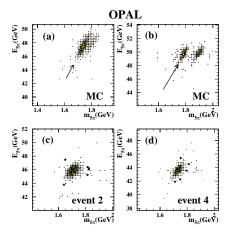


FIG. 2. The results of the Monte Carlo cloning technique applied to two Monte Carlo events with reconstruction problems are shown in figures (a) and (b); the beginning of the arrow shows the generated values of M_h and E_h , the end of the arrow shows values of these quantities after the first Monte Carlo reconstruction and the boxes show the distribution of these quantities obtained by applying the Monte Carlo cloning technique to these two events. The result of the same technique applied to the two most sensitive data events is shown in figures (c) and (d).

Typical mass and energy resolutions of the OPAL analysis are 20-25 MeV and 500 MeV respectively. The fit to the 22 OPAL events gives a limit of $m_{\nu_{\tau}} < 39.6$ MeV at 95% confidence level. As for ALEPH the systematic error is dominated by the knowledge of the resolution function parameters and is of 3.6 MeV. By adding linearly this systematics to statistical limit OPAL obtains a 95 % C.L. upper limit on $m_{\nu_{\tau}}$ of 43.2 MeV.

B. Results form $\tau \to 3\pi^{\pm}\nu_{\tau}$ tau decays

As mentioned in the introduction the three-prong tau decay mode is competitive with the five-prong one in the determination of the tau neutrino mass. The three LEP experiments ALEPH [10], DELPHI [11] and OPAL [12] have used this decay mode to constraint the tau-neutrino mass.

The ALEPH results is based on a fit to the M_h, E_h distribution. Due to the large statistics the fit has been limited to an high M_h, E_h region where 3000 $\tau \to 3\pi^{\pm}\nu_{\tau}$ decays have been selected. The selection efficiency in this region is of about 49% with a background from dangerous topologies of less then 0.2%. The high statistics of this channel make

the cloning technique not viable. For this reason ALEPH has parameterised the quantities entering in resolution \mathcal{R} as a function of the hadronic mass and energy. The typical values of the mass and of the energy resolution are similar to the ones obtained in the five-prong mode. The fit gives a statistical limit of 21.5 MeV on the tau-neutrino mass at 95% confidence level. The systematic error on this limit is again dominated by the knowledge of the resolution function and ammount to 4.2 MeV. This error is larger than the five-prong one mainly because of the non use of the cloning technique. Adding linearly the systematic error to the fit result a 95% C.L. limit of $m_{\nu_{\tau}} < 25.7$ MeV has been obtained.

The OPAL experiment has tried to increase its sensitivity to the tau neutrino mass by partially reconstructing the tau direction in three-prong versus three-prong tau events. In this kind of events the thrust axes is a good approximation of the tau direction especially for events where the three-prong are very energetic. By a fit to the two variables square missing-mass and missing-energy on a sample of 2514 events OPAL obtained an upper limit of 32.1 MeV at 95% C.L. on $m_{\nu_{\tau}}$. The systematic error has been estimated to be of 3.2 MeV dominated by the knowledge of the resolution function parameters. This gives a final limit of $m_{\nu_{\tau}} < 35.3$ MeV at 95% confidence level.

The DELPHI experiment has selected 12538 $\tau \to 3\pi^{\pm}\nu_{\tau}$ decays with a 38% efficiency and a dangerous background of 1.5 %. A fit to the M_h , E_h distribution gives a 95 % C.L. upper limit of 25 MeV on the tau-neutrino mass. In the study of the systematics DELPHI has observed a significant disagreement between the three-prong mass spectrum in the data sample and the one obtained with a Monte Carlo based on the Kün-Satamaria model [13]. This discrepancy is observed in the M_h range (1.5-1.9) GeV. The DELPHI collaboration claimed [14] that this excess could be explained if about 2.3% of new resonance, the a'(1700) with a mass of 1.7 GeV and a width of 0.3 GeV, was added in the three-prong tau decay. The description to the Dalitz plots in the three-prong tau decays also improved by the addition of this resonance. The CLEO experiment has tried to measure the ammount of this resonance in their three-prong tau sample [15] (by assuming a massless tau-neutrino) and has obtained (with different models) an a'(1700) fraction of the order of (0.1-0.4)% which is significantly smaller than the 2.3% reported by DELPHI.

The ALEPH and the OPAL experiments has observed the same problem as DELPHI in describing the $\tau \to 3\pi^{\pm}\nu_{\tau}$ Dalitz plots however the do not observe any excess with respect to the Khün and Santamaria model in the hadronic mass spectrum. The ALEPH experiment has checked the effect of such a large ammount of a'(1700) on its limit: if a 2.5% of a'(1700) with the parameters suggested by DELPHI is added in the three-prong fit the limit on $m_{\nu_{\tau}}$ is worsened by about 6 MeV. This implies a variation on the combined three- and five-prong ALEPH upper limit, reported in the following, of about 1 MeV.

As DELPHI correctly states that a simultaneous fit of the a'(1700) properties and of $m_{\nu_{\tau}}$ in three-prong tau decays is not possible. In view of the CLEO results and of the ALEPH check is unlikely that the limit on the tau neutrino mass can be deteriorated by the presence of this new resonance. More inputs from theorists is welcome.

C. Combination of the ALEPH and OPAL results

The ALEPH and the OPAL collaborations have combined [10,6] (separately) their three- and five-prong upper limits on the tau-neutrino masses. The method used to combine these results is based on the likelihood product. In doing the combination the correlation between the systematic errors of the two decay modes has been properly taken into account as described in [10,6]. The limit obtained by the OPAL and by the ALEPH collaborations are respectively of $m_{\nu_{\tau}} < 27.6$ MeV and of $m_{\nu_{\tau}} < 18.2$ MeV at 95% confidence level, including systematic effects.

The results from the different LEP experiments and from the different tau decay modes are limited by statistics. Moreover the dominant systematics (resolution function parameters) are mainly uncorrelated between the different LEP experiments. For this reason a combination of the LEP results would improve the sensitivity to the tau-neutrino mass. I have done this exercise in order to get an estimate of what this combined limit would be. I have used the five- and three-prong likelihoods published by the ALEPH and by the OPAL experiments (the DELPHI results have not yet been published). The method is the same as the one used in the ALEPH and OPAL publications:

$$\mathcal{L}_{COMB}(m_{\nu}) = \mathcal{L}_{OPAL}^{3\pi}(m_{\nu}) \times \mathcal{L}_{OPAL}^{5\pi}(m_{\nu}) \times \mathcal{L}_{ALEPH}^{5\pi}(m_{\nu}) \times \mathcal{L}_{ALEPH}^{3\pi}(m_{\nu})$$
 (2)

the combined likelihood is shown in Fig. 3.

From this likelihood a 95% C.L. limit $m_{\nu_{\tau}} < 13.6$ MeV can be derived by requiring $ln(\mathcal{L}(m_{\nu}^{95})) = ln(\mathcal{L}^{MAX}) - 1.92$ (this method is almost equivalent to the one based on the integration of the likelihood, used for example by CLEO, when the likelihood shape is fairly Gaussian as in this case).

To estimate the systematic error all the modified likelihoods containing the effect of the different systematic sources would be needed. Since they are not published a rough estimate of the systematics have been obtained by multiplying each likelihood by a constant factor which brings, for each channel, the limit on $m_{\nu_{\tau}}$ to be equal to the ones which includes the systematics. The total systematics has been obtained as followed: the systematic error for each combined mode is obtained by subtracting to the limit derived with the modified likelihoods the one obtained without systematics; all these errors are added in quadrature (in this way the possible correlations between the different systematic errors are not taken into account) giving a total systematics of 1.4 MeV. By adding linearly this error the the statistical result a combined ALEPH+OPAL 95% C.L upper limit of 15 MeV on $m_{\nu_{\tau}}$ is obtained. I want to stress that this combination is unofficial and approximated. The aim is to give an idea of the gain which could be achieved with the combination of the LEP results and to push the ALEPH, DELPHI and OPAL collaboration to produce an official combined $m_{\nu_{\tau}}$ limit.

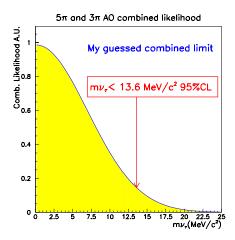


FIG. 3. The ALEPH and OPAL combined likelihood as a function of $m_{\nu_{\tau}}$ obtained from five- and three-prong published results. This likelihood does not include systematic effects.

IV. COMPARISON WITH CLEO RESULTS

The CLEO experiment has collected a huge statistics of tau decays at a centre-of-mass energy close to the $\Upsilon(4s)$ resonance and is expected to have a sensitivity to $m_{\nu_{\tau}}$ larger than that of the LEP experiments. The performance of the CLEO [16], ALEPH [7] and OPAL [6] 5π analyses are compared in table I. The CLEO limits are worse than the ALEPH one even though the CLEO statistics is a factor of five larger. This brings to the question: is CLEO unlucky or the are LEP results lucky? It would be nice to evaluate for each experiment the expected limit on $m_{\nu_{\tau}}$. Its comparison with the actual one will tell us who is lucky and who is unlucky. Unfortunately the unknown hadronic dynamics doesn't allow the evaluation of the a priori sensitivity of an experiment. The ALEPH experiment claims that the probability to get such a lucky distribution in the M_h , E_h plane is at the level of 15% if a model of the dynamics driven by $\pi\pi a_1$ is assumed in 5π tau decays. At the same time CLEO claims that the probability to get a limit on $m_{\nu_{\tau}}$ such a bad or worse than what they have obtained is at the level of 23% if a softer mass spectrum is assumed in the five-prong tau decays. So the puzzle stays unsolved. What can be done is to compare data with

data in the region where they are more sensitive to the tau-neutrino mass. This exercise is shown in Fig. 4 where the number of 5π events are plotted in slices of iso- $m_{\nu_{\tau}}$ in the M_h, E_h plane; in order to have more statistics the ALEPH and the OPAL events have been summed up in this comparison.

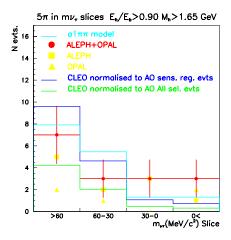


FIG. 4. The LEP (ALEPH+OPAL) five-prong events compared with the CLEO ones in terms of $m_{\nu_{\tau}}$ slices in the M_h, E_h plane after requiring $M_h > 1.65$ GeV and $E_h/E_b > 0.9$. The red dots represents the LEP events. The dark-blue histogram shows the CLEO events normalised to the number of LEP events in this *sensitive* region. The green histogram shows the CLEO events normalised to the total number of LEP selected events. The ligh-blue histogram shows the expected events obtained by using a $\pi\pi a_1$ model for the five-prong tau decay.

Only the events in a sensitive region which corresponds to $M_h > 1.65$ GeV and $E_h/E_b > 0.9$ are shown. The selection efficiency is assumed to be flat in the full M_h, E_h plane. It finds out from this plot that the shapes of the LEP and CLEO data are compatible. This is shown by the comparison between the dark-blue line and the red dots of Fig. 4; the CLEO events in the sensitive region have been normalised the number of ALEPH+OPAL events in the same region.

For what concerns the fraction of 5π events selected in this region with respect to the total number of selected 5π events the compatibility is less good as can be observed by comparing the green line in Fig. 4 with the red dots; the ALEPH and the OPAL experiments select a total of 16 events in this *sensitive* region which should be compared with about 7 which is the number of events observed by CLEO in this *sensitive* region rescaled to the ALEPH+OPAL 5π statistics. These two numbers are barely compatible. The number of *expected* events normalised to the ALEPH plus OPAL statistics is of about 18 with the $\pi\pi a_1$ dynamics (this is showed by the light-blue line of Fig. 4) and of about 9 with a softer dynamics similar to phase-space.

Even more intriguing is the fact that the likelihood shown by the CLEO experiment at the TAU98 workshop [17] shows a peak at $m_{\nu_{\tau}} \sim 18$ MeV. This likelihood is preliminary and doesn't include the systematic errors. If the ALEPH method described above is applied to this likelihood the value of $m_{\nu_{\tau}} = 0$ is excluded at more than 90 % confidence level. This could mean that CLEO is on the verge of a very interesting result or that (more probably but less interesting) there is in the CLEO likelihood a bias towards large neutrino masses. This bias would make the CLEO limit more conservative (explaining why their limit is so unlucky) and is therefore not warring in terms of the validity of their $m_{\nu_{\tau}}$ upper limit. One should remember that most of the systematics determined by the different experiments are studied in terms of bias towards a massless tau-neutrino while less attention is played to possible sources which can mimic a massive neutrinos. A typical example is the fact that all the experiments reduce the dangerous background (the one which can mimic a massless tau-neutrino) at the 1-2% level while backgrounds as high as 10% from higher decay multiplicities (like a $3\pi^{\pm}\pi^{0}$ reconstructed as a $3\pi^{\pm}$ tau decays) which can mimic a massive

neutrino are accepted. The CLEO experiment as still a large fraction of its statistics to analyse so I think that this intriguing situation will be clarified soon.

TABLE I. Comparison between the performance of LEP and CLEO 5π analyses. For the different analyses the mass resolution in Mev, the energy resolution divided by the beam energy, the number of selected events, the efficiency in per cent and the 95 % upper limit, statistical only, on $m_{\nu_{\tau}}$ in MeV are reported.

	$\sigma(M_h) \text{ GeV}$	$\sigma(E_h)/E_{beam}$	N evts	Efficiency %	$m_{\nu}^{95}~{ m MeV}$
ALEPH $5\pi^{\pm}$	10-15	0.35/45.6	52	27	22.3
OPAL $5\pi^{\pm}$	20-25	0.5/45.6	22	9	39.6
CLEO $5\pi^{\pm}$	15	0.025/10.	266	3	31.0
CLEO $3\pi^{\pm}2\pi^{0}$	25	0.05/10.	207	0.4	33.0

V. CONCLUSIONS AND ACKNOWLEDGEMENTS

The LEP experiments have put constraints on $m_{\nu_{\tau}}$ by fitting the M_h, E_h distribution in three- and five-prong tau decays. The best results obtained by a single experiment is given by ALEPH which obtains $m_{\nu_{\tau}} < 18.2$ MeV at 95% confidence level by combining the three- and five-prong results.

An unofficial combination of the ALEPH and OPAL results shows that LEP can exclude at 95% C.L. values of $m_{\nu_{\tau}}$ higher than 15 MeV. In my personal opinion the CLEO experiment has the statistical power to go below this limit.

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