

# Influence of Parton $k_T$ on High- $p_T$ Particle Production

Michael Begel  
*University of Rochester*  
*Rochester, NY 14627 USA*

FOR THE E706 COLLABORATION

We report on recent work concerning the phenomenology of initial-state parton- $k_T$  effects in direct-photon production and related processes in hadron collisions. High-mass direct-photon and  $\pi^0$  pairs are used to explore the impact of parton- $k_T$  on kinematic distributions. After a brief summary of a phenomenological  $k_T$ -smearing model, we present a study of recent results on fixed-target and collider direct-photon production. This approach provides a consistent description of the observed deviations of next-to-leading order QCD calculations relative to the inclusive direct-photon and  $\pi^0$  data. We also comment on the implications of these results for the extraction of the gluon distribution of the nucleon.

## I. INTRODUCTION

Direct-photon production has long been viewed as an ideal process for measuring the gluon distribution in the proton and has been calculated within perturbative QCD (pQCD) to next-to-leading order (NLO) [1]. The quark-gluon Compton scattering subprocess ( $gq \rightarrow \gamma q$ ) provides a large contribution to inclusive direct-photon production. The gluon distribution is relatively well constrained for  $x < 0.1$  by deep-inelastic scattering and Drell-Yan data, but less so at larger  $x$ . Direct-photon data can constrain the fits at large  $x$ , and consequently has been incorporated in several modern global parton distribution analyses.

A pattern of deviation between measured direct-photon cross sections and NLO calculations has been observed [2]. The suspected origin of the disagreements is the effect of initial-state soft-gluon radiation, referred to here as  $k_T$ -effects. Kinematic distributions of high-mass pairs of particles directly probe the transverse momentum of incident partons in hard-scattering events. Evidence of significant  $k_T$  has been observed in measurements of dimuon, diphoton, and dijet pairs [3]. A collection of measurements of the average transverse momentum of the pairs ( $\langle p_T \rangle_{pair}$ ) is displayed in Fig. 1 (left) for a wide range of center-of-mass energies ( $\sqrt{s}$ ). The values of  $\langle p_T \rangle_{pair}$  are large, and increase with increasing  $\sqrt{s}$ . The values of  $\langle k_T \rangle$  per parton (estimated as  $\approx \langle p_T \rangle_{pair} / \sqrt{2}$ ) indicated by these Drell-Yan, diphoton, and dijet data, as well as the inclusive direct-photon and  $\pi^0$  production data, are too large to be interpreted as “intrinsic” — i.e., due only to the finite size of the proton. From the observed data, one can infer that the average  $k_T$  per parton is order 1 GeV/ $c$  at fixed-target energies, increasing to 3-4 GeV/ $c$  at the Tevatron collider, while one would expect  $\langle k_T \rangle$  values on the order of 0.3 to 0.5 GeV/ $c$  based solely on proton size.

## II. COMPARISONS WITH E706

Fermilab E706 is a fixed-target experiment designed to measure the production of direct photons, neutral mesons, and associated particles at high  $p_T$  [4]. The apparatus included a charged particle spectrometer consisting of silicon microstrip detectors in the target region and multiwire proportional chambers and straw tube drift chambers downstream of a large aperture analysis magnet [5]. Photons were detected in a large, lead and liquid-argon, sampling electromagnetic calorimeter (EMLAC), located 9 m downstream of the target [6]. The EMLAC readout was split azimuthally into octants, each consisting of interleaved, finely segmented, radial and azimuthal views. The radial views were also used to form a fast, localized, high- $p_T$  event selection trigger. Correlations between localized high- $p_T$  electromagnetic depositions on opposite sides of the EMLAC were used to trigger on the production of high-mass pairs of neutral particles. The experiment accumulated data from a 515 GeV/ $c$   $\pi^-$  beam, and from 530 GeV/ $c$  and 800 GeV/ $c$  proton beams incident upon beryllium, copper, and hydrogen targets.

## A. High-Mass Pairs

The distributions of high-mass direct-photon pairs as functions of pair  $p_T$  ( $Q_T$ ), azimuthal angle between the photons ( $\Delta\phi$ ), and out-of-plane momentum ( $p_{OUT}$ ) are shown in Fig. 1 (right) for 515 GeV/c  $\pi^-$ -Be interactions. Overlaid on the data are the results from both NLO [7] and resummed [8] pQCD calculations. The shape of the NLO calculation is inconsistent with the data distributions. The resummed calculation (RESBOS), which incorporates the effects of multiple soft-gluon emission, provides a reasonable match to the shape of the data. Also shown are the double direct-photon distributions from PYTHIA, which approximates  $k_T$  effects by a Gaussian smearing technique. PYTHIA provides a reasonable description of the data using a value for  $\langle k_T \rangle$  consistent with the measurements displayed in Fig. 1.

Analyses of high-mass  $\pi^0$  pairs [4], as well as studies of the distribution of the fractional momentum carried by charged particles in jets recoiling against isolated photons, also show evidence of substantial  $k_T$ , as do our comparisons of the measured high- $p_T$  charged-D cross section to NLO pQCD [5]. All these results suggest a supplemental  $\langle k_T \rangle$  of order 1 GeV/c. Similar soft-gluon effects may be expected in other hard-scattering processes, such as the inclusive production of jets or direct photons [9–11].

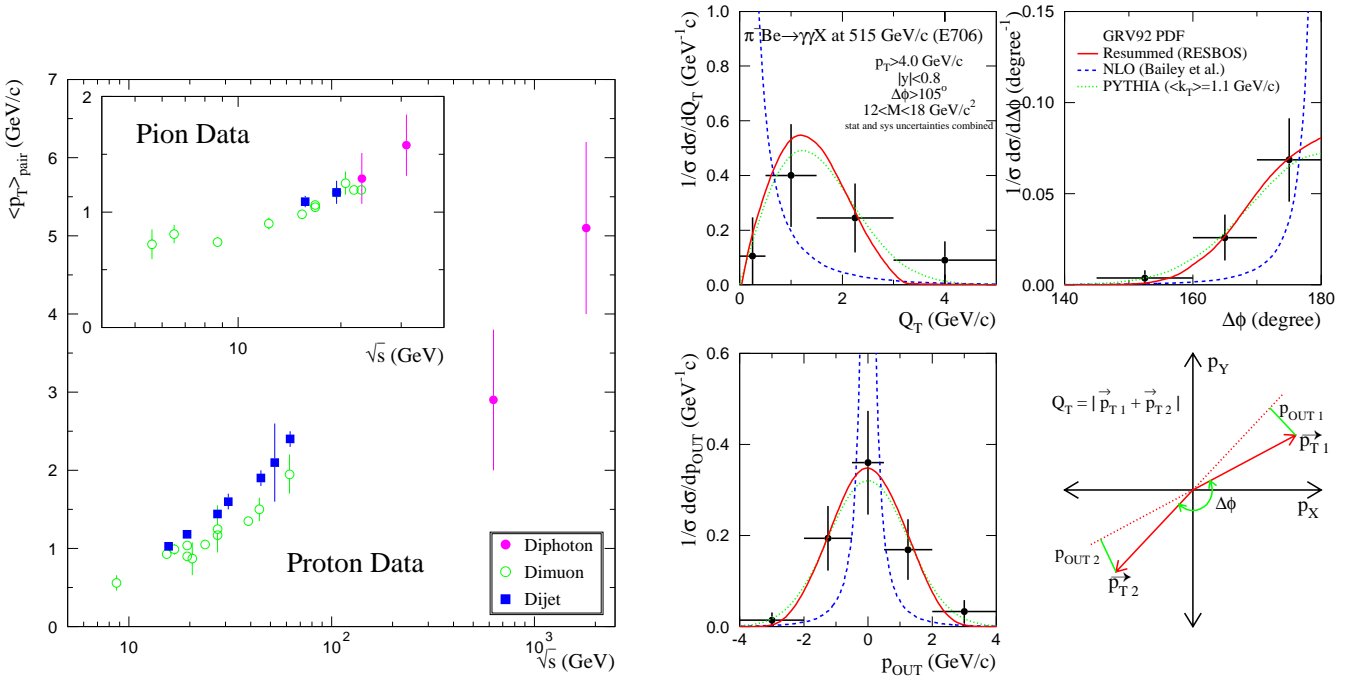


FIG. 1. Left:  $\langle p_T \rangle$  of pairs of muons, photons, and jets produced in hadronic collisions by incident protons or pions versus  $\sqrt{s}$  ( $\langle p_T \rangle_{pair} \approx \sqrt{2} \langle k_T \rangle$ ).

Right: Kinematic distributions (preliminary) for high-mass direct-photon pairs produced in 515 GeV/c  $\pi^-$ -Be interactions. Overlaid on the data are the results from NLO (dashed) and resummed (solid) calculations. PYTHIA results (dotted) with  $\langle k_T \rangle = 1.1$  GeV/c are also shown. The various kinematic quantities are illustrated in the vector diagram.

## B. Inclusive Production

Invariant cross sections for inclusive direct-photon and  $\pi^0$  production are displayed in Figs. 2 and 3 with theory overlays. Discrepancies between the NLO theory and the data are particularly striking. Resummed pQCD calculations for single direct-photon production are anticipated [12–14]. Since current NLO theory calculations do not account for

the effects of multiple soft-gluon emission, we employed a phenomenological model to incorporate  $k_T$  effects in pQCD calculations of direct-photon and  $\pi^0$  production [4,3].

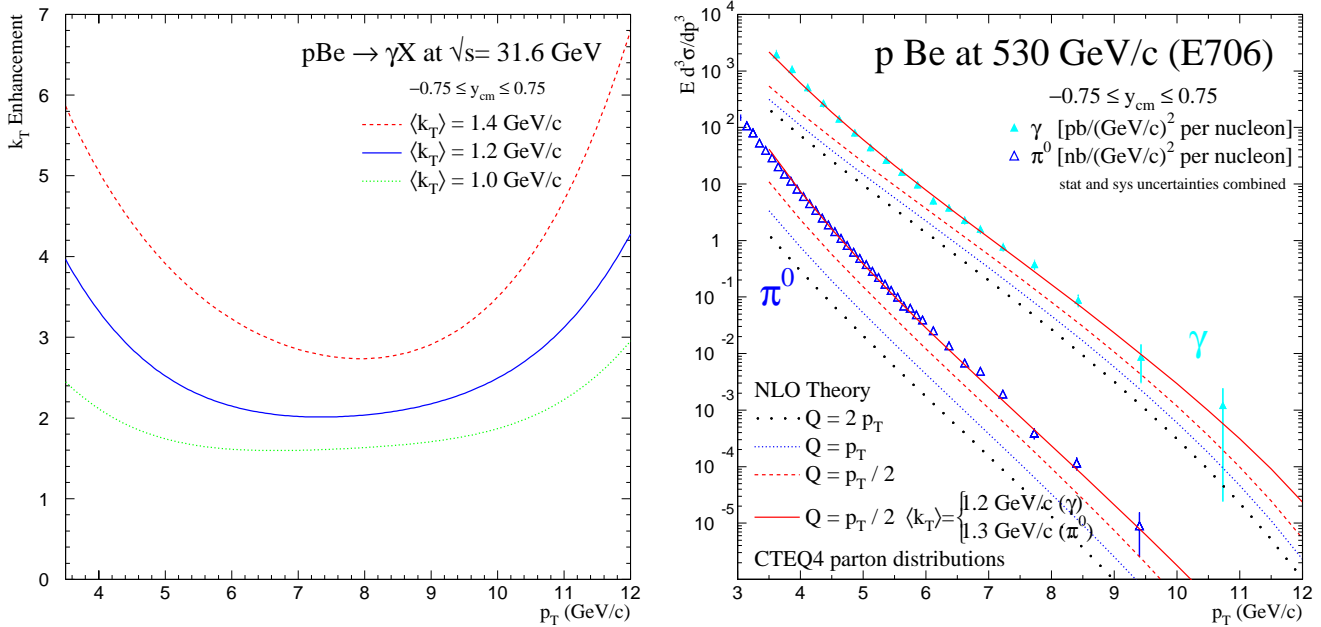


FIG. 2. Left: The variation of  $k_T$  enhancements,  $K(p_T)$ , relevant to the E706 direct-photon data in the figure to the right. Right: Invariant cross sections (per nucleon) for direct-photon and  $\pi^0$  production in pBe interactions at 530 GeV/c. Cross sections are shown as a function of  $p_T$  averaged over the full rapidity range. Curves represent NLO QCD calculations for scale choices of  $Q = 2p_T$  (wide dots),  $Q = p_T$  (dotted), and  $Q = p_T/2$  (dashed), and a  $k_T$ -enhanced NLO result with scale  $Q = p_T/2$  (solid).

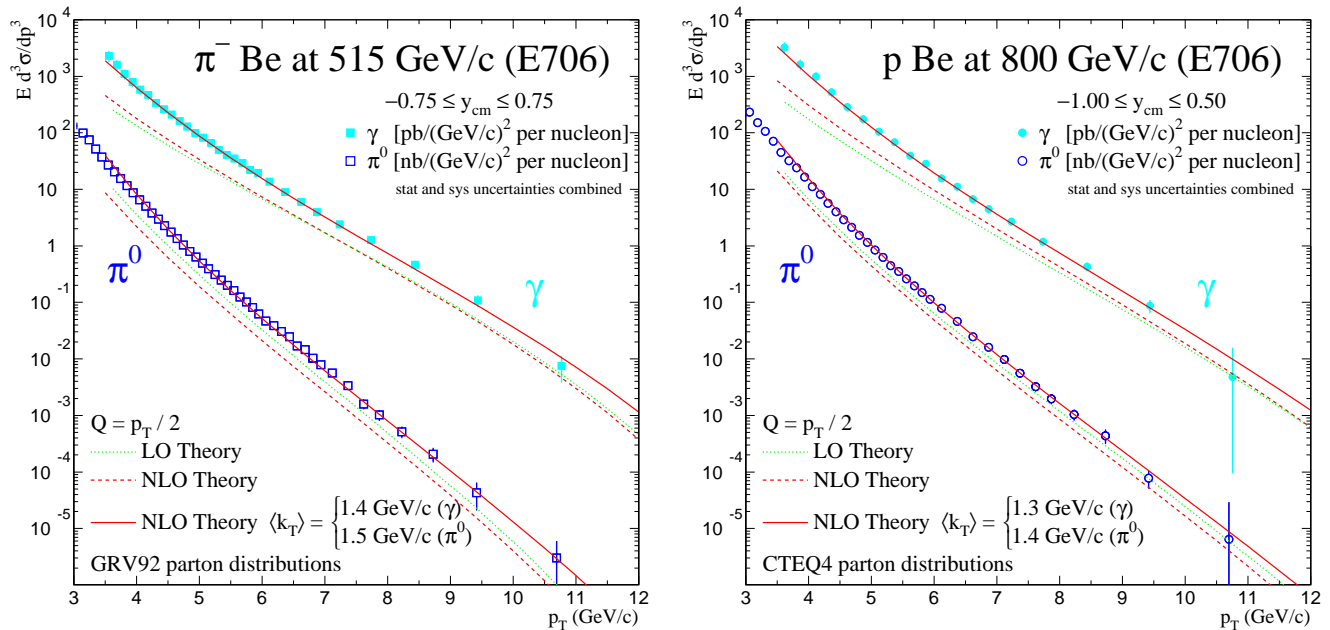


FIG. 3. Invariant cross sections (per nucleon) for direct-photon and  $\pi^0$  production in  $\pi^-$ Be interactions at 515 GeV/c (left) and pBe interactions at 800 GeV/c (right). Cross sections are shown as a function of  $p_T$  averaged over the full rapidity range. Curves represent LO (dotted) and NLO (dashed) pQCD calculations and a  $k_T$ -enhanced NLO result for scale  $Q = p_T/2$ .

We use leading-order (LO) pQCD calculations [15] which include Gaussian  $k_T$  smearing to create K-factors (Fig. 2), and then apply these K-factors to the NLO calculations. We recognize that this procedure involves a risk of double-counting since some of the  $k_T$ -enhancement may already be contained in the NLO calculation. However, we expect such double-counting effects to be small. The  $k_T$ -enhancements (using values consistent with the high-mass pair data) are successful in describing both the shape and normalization of both the direct-photon and  $\pi^0$  cross sections (Figs. 2 and 3).

### III. COMPARISONS WITH OTHER EXPERIMENTS

We can use this phenomenological  $k_T$  model to compare with cross sections from other experiments. The consequences of  $k_T$  smearing are expected to depend on  $\sqrt{s}$  (Fig. 1). At the Tevatron collider [16], where  $p_T$  is large compared to  $k_T$ , the above model of soft-gluon radiation leads to a relatively small modification of the NLO cross section. Only the lowest end of the  $p_T$  spectrum is significantly modified (Fig. 4). CDF has measured an average transverse momentum of photon pairs of  $\langle p_T \rangle_{pair} = 5.1 \pm 1.1$  GeV/ $c$  at  $\sqrt{s} = 1.8$  TeV [17]. Employing this value, the phenomenological model adequately describes the excess of data over NLO theory at low- $p_T$  for both CDF and D0. The agreement between the phenomenological model and the collider direct-photon data can also be seen in preliminary CDF data at  $\sqrt{s} = 630$  GeV (Fig. 4 (right)).

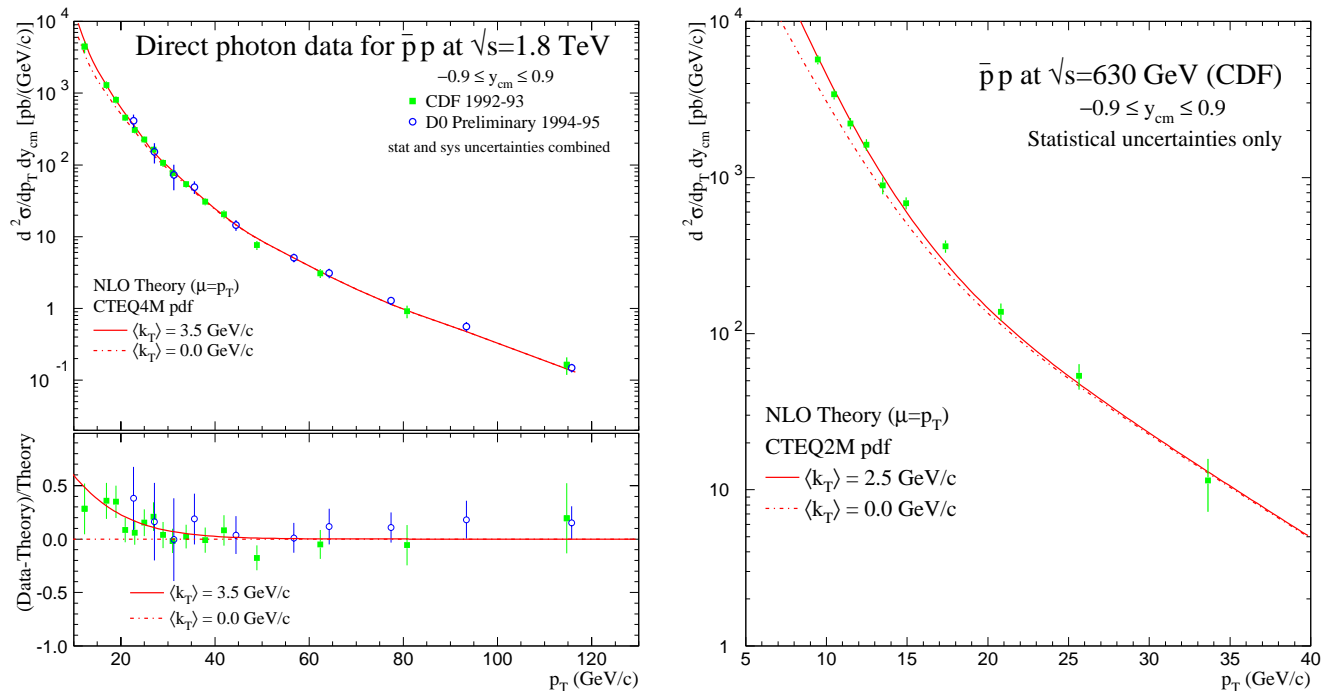


FIG. 4. Left: Isolated direct-photon cross sections from CDF and D0 at  $\sqrt{s} = 1.8$  TeV. Overlaid on the data are the results of the NLO calculations with (solid) and without (dashed)  $k_T$  enhancements for  $\langle k_T \rangle = 3.5$  GeV/ $c$ . Right: Preliminary, isolated direct-photon cross section for CDF at  $\sqrt{s} = 630$  GeV. Overlaid on the data are the results of the NLO calculations with (solid) and without (dashed)  $k_T$  enhancements for  $\langle k_T \rangle = 2.5$  GeV/ $c$ .

Comparisons are also shown for the lower energy WA70 [18] (Fig. 5) and UA6 [19] data (Fig. 6). Both WA70 and UA6 have measured direct-photon and  $\pi^0$  production with good statistics, and their direct-photon data have been included in recent global parton distribution fits. The center-of-mass energies for these two experiments ( $\sqrt{s} \approx 24$  GeV) are lower than those for E706. Correspondingly,  $\langle k_T \rangle$  values for these experiments are expected to be slightly smaller than the values used for E706. WA70 measured  $\langle k_T \rangle = 0.9 \pm 0.1 \pm 0.2$  GeV/ $c$  using their diphoton sample [20]. We therefore use this  $\langle k_T \rangle$  as the central value for the  $k_T$ -enhancement factors for both experiments and vary the  $\langle k_T \rangle$

by  $\pm 0.2$  GeV/ $c$  (Figs. 5 and 6). Over the narrower  $p_T$  range of the WA70 and UA6 measurements, the effect of  $k_T$  is essentially to produce a shift in normalization. The  $k_T$ -enhanced theory compares well with the  $\pi^0$  cross sections and with the UA6 and  $\pi^-$  beam WA70 direct-photon cross sections.

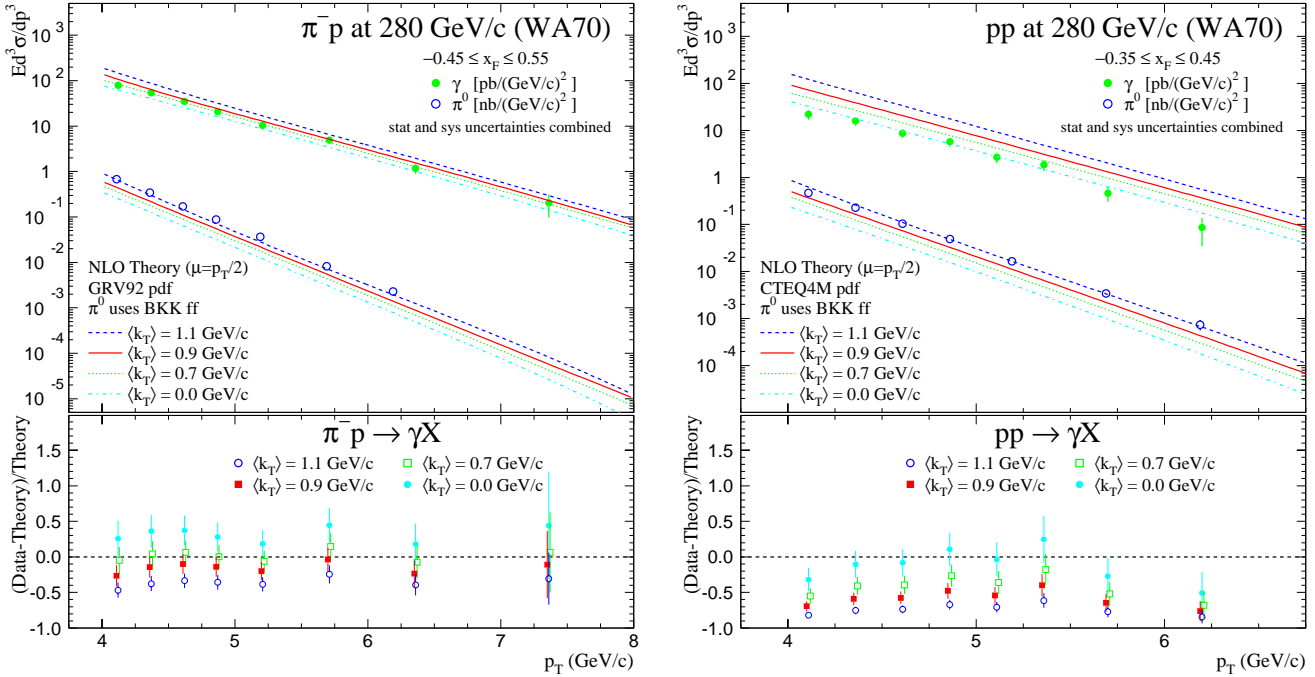


FIG. 5. Invariant cross sections for direct-photon and  $\pi^0$  production from WA70. Overlaid on the data are the results of the NLO calculation with  $k_T$  enhancements for several values of  $\langle k_T \rangle$ . A linear comparison is shown for the direct-photon data.

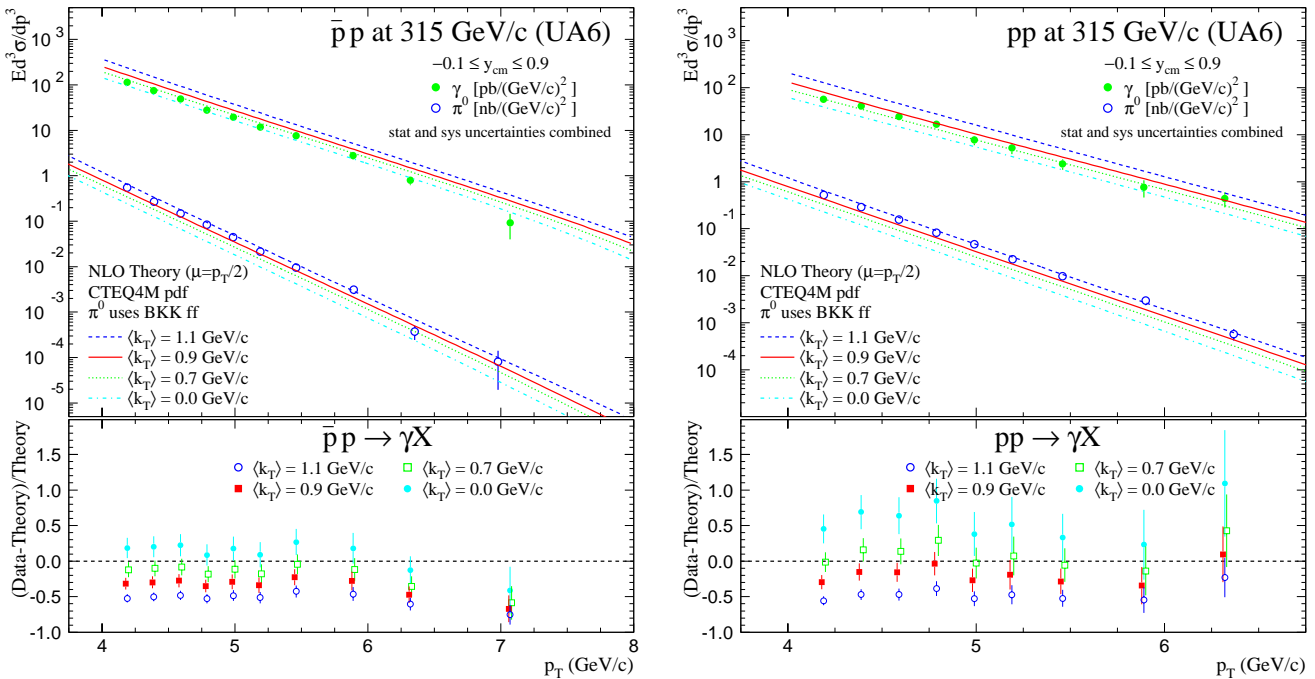


FIG. 6. Invariant cross sections for direct-photon and  $\pi^0$  production from UA6. Overlaid on the data are the results of the NLO calculation with  $k_T$  enhancements for several values of  $\langle k_T \rangle$ . A linear comparison is shown for the direct-photon data.

#### IV. GLUON DISTRIBUTION

It is generally accepted that the uncertainty on the gluon distribution at large  $x$  is still quite large [21]. Thus, it is important to incorporate further constraints on the gluon, especially from direct-photon data. To investigate the impact of  $k_T$  effects on determinations of the gluon distribution, we have included the E706 direct-photon cross sections for incident protons, along with deep-inelastic scattering and Drell-Yan data that were used in determining the CTEQ4M PDFs, in a global fit to the parton distribution functions. The CTEQ fitting package was employed to obtain these results [22], using the NLO pQCD calculations for direct-photon cross sections, adjusted by the  $k_T$ -enhancement factors. The WA70, UA6, CDF, and D0 direct-photon and jet data were excluded from this particular fit. The resulting gluon distribution, shown in Fig. 7, is similar to CTEQ4M, as expected, since the  $k_T$ -enhanced NLO calculations using CTEQ4M provide a reasonable description of the E706 data (Figs. 2 and 3).

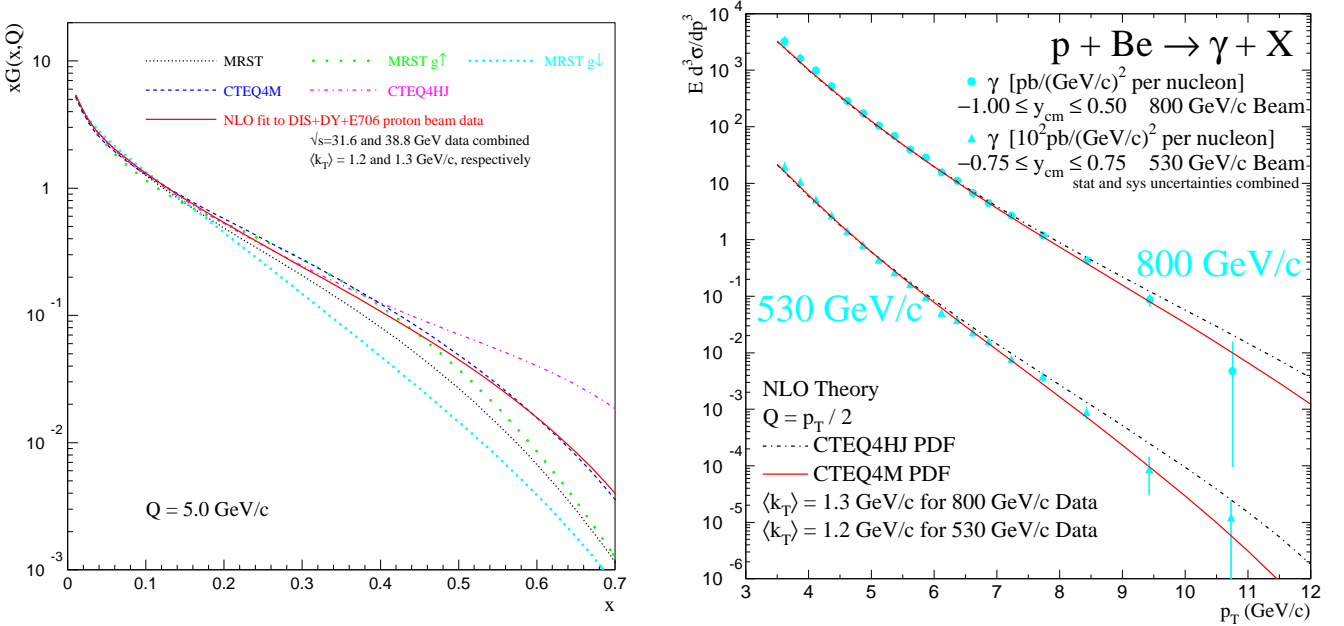


FIG. 7. Left: A comparison of the CTEQ4M, MRST, and CTEQ4HJ gluons, and the gluon distribution derived from fits that use E706 data. The  $g \uparrow$  and  $g \downarrow$  gluon densities correspond to the maximum variation in  $\langle k_T \rangle$  that MRST allowed in their fits.

Right: The invariant direct-photon cross-section from the E706 proton beam data overlayed with  $k_T$ -enhanced NLO calculations using CTEQ4M (solid) and CTEQ4HJ (dash-dot) PDFs.

The MRST gluon distribution [23] (also shown in Fig. 7) is significantly lower than CTEQ4M at large  $x$ . While the MRST fit employs  $k_T$  enhancements (obtained using a different, analytical integration, technique), it attempts to accommodate the WA70 incident-proton direct-photon data, which does not exhibit an obvious  $k_T$  effect [24] (Fig. 5). In contrast, the CTEQ4HJ gluon distribution [22], designed to improve the description of the high- $p_T$  jet data from CDF, is much larger than CTEQ4M in the same  $x$  range. (A comparison between the E706 direct-photon data and the calculations using CTEQ4M and CTEQ4HJ PDFs is shown in the right-side of Fig. 7 to illustrate the sensitivity of the direct-photon data to the gluon distribution.) This spread of solutions for the gluon distribution is uncomfortably large, and additional theoretical work is warranted to properly incorporate the available direct-photon data in the PDF fits.

## V. CONCLUSION

Discrepancies between NLO pQCD calculations and direct-photon cross sections have been observed; they are particularly striking in the high statistics data from E706. The suspected origin of the disagreements is from the effects of initial-state soft-gluon radiation. A resummed pQCD calculation, which incorporates the effects of multiple soft-gluon emission, is sufficient to describe the shapes of kinematic distributions of high-mass direct-photon pairs. Pending completion of resummed calculations for inclusive direct-photon production, we employed a phenomenological model to incorporate  $k_T$  effects in pQCD calculations of direct-photon and  $\pi^0$  production. Using  $\langle k_T \rangle$  values consistent with the high-mass pair data, we find that the  $k_T$ -enhanced theory compares well with the  $\pi^0$  cross sections and with the CDF, D0, E706, UA6, and  $\pi^-$  beam WA70 direct-photon cross sections. Further theoretical work in this area would be valuable for reducing the uncertainties on the gluon distribution at medium to high  $x$ .

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